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The Crystal Structure of Sborgite, $\text{NaB}_5\text{O}_6(\text{OH})_4 \cdot 3\text{H}_2\text{O}$

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The crystal structure of sborgite (space group $C2/c$, cell parameters $a=11.119$, $b=16.474$, $c=13.576$ Å, $\beta=112^\circ 50'$) was determined by the symbolic addition method and refined by the least-squares method (with anisotropic thermal parameters for non-hydrogen atoms) to a final R value of 0.062. The structure contains the pentaborate ion $[\text{B}_5\text{O}_6(\text{OH})_4]^-$ characterized by the double ring built up from one BO_4 tetrahedron and three BO_3 triangles. The two sodium ions in the asymmetric unit are in special positions along a binary axis: one is octahedrally coordinated by four water molecules and two hydroxyl ions, the other is tetrahedrally coordinated by two water molecules and two hydroxyl ions, with two more distant contacts at nearly 3 Å. A complex system of hydrogen bonds connects the pentaborate ions and the sodium coordination polyhedra.

Introduction

Sborgite was reported as a new mineral phase by Cipriani (1957) who found it associated with borax and thenardite among the compounds incrusting the training pipes of some 'soffioni' in the boriferous area of Larderello. Cipriani identified it, on the basis of its powder diffraction pattern, optical data and density, with the compound $\text{NaB}_5\text{O}_8 \cdot 5\text{H}_2\text{O}$, synthesized and studied by Sborgi in his researches on the ternary system $\text{Na}_2\text{O}-\text{B}_2\text{O}_3-\text{H}_2\text{O}$. The cell data and space group were determined by Sabelli (1962).

Christ (1960), in his study on the crystal chemistry of hydrated borates, advanced the hypothesis that sborgite must contain the pentaborate ion $[\text{B}_5\text{O}_6(\text{OH})_4]^-$, known to exist, to that date, in the compound $\text{NH}_4\text{B}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$ and in its potassium analogue $\text{KB}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$ (Zachariasen, 1937). Recently we found this same group isolated, or variously polymerized, in some minerals and artificial products (Merlino, 1969; Merlino & Sartori, 1969, 1971). We were thus strongly motivated to undertake the structural study of sborgite in order to define its position in the crystal-chemical classification of borates and its relations with the other compounds containing the pentaborate group.

Experimental

Synthetic crystals of sborgite, suitable for X-ray single-crystal investigations, were obtained following the suggestions of Cipriani (1957). Unit-cell constants were determined from the least-squares refinement of powder data.

Sborgite, $\text{NaB}_5\text{O}_8 \cdot 5\text{H}_2\text{O}$ M.W. 295.17
Monoclinic, space group $C2/c$ or Cc ($C2/c$ established by intensity statistics)

$$\begin{aligned} a &= 11.119 \text{ (8) } \text{ \AA} \\ b &= 16.474 \text{ (14) } \\ c &= 13.576 \text{ (9) } \\ \beta &= 112^\circ 50' \text{ (2)'} \end{aligned}$$

Unit-cell volume, $V=2291.9 \text{ \AA}^3$ $Z=8$
 $D_m=1.713 \text{ g.cm}^{-3}$, as determined by Sabelli, $D_c=1.711 \text{ g.cm}^{-3}$, $F(000)=1200$, $\mu=17.0 \text{ cm}^{-1}$ (Cu $K\alpha$).

The intensity data were recorded with nickel-filtered Cu $K\alpha$ radiation ($\lambda=1.5418 \text{ \AA}$), by means of Weissenberg photographs, with the multiple-film technique and integration process. A fragment elongated in the a direction was cut from a large crystal and reduced to cylindrical shape with cross sectional radius of 0.025 cm ($\mu R=0.382$ for Cu $K\alpha$ radiation). Eleven layers with a as rotation axis ($h=0$ through 10) were recorded

Table 3 (cont.)

h	k	l	F _o	F _c	ΔF	σ _F	σ _w	σ _{ΔF}
0	0	0	1000	1000	0	0	0	0
0	1	0	1000	1000	0	0	0	0
0	2	0	1000	1000	0	0	0	0
0	3	0	1000	1000	0	0	0	0
0	4	0	1000	1000	0	0	0	0
0	5	0	1000	1000	0	0	0	0
0	6	0	1000	1000	0	0	0	0
0	7	0	1000	1000	0	0	0	0
0	8	0	1000	1000	0	0	0	0
0	9	0	1000	1000	0	0	0	0
0	10	0	1000	1000	0	0	0	0
0	11	0	1000	1000	0	0	0	0
0	12	0	1000	1000	0	0	0	0
0	13	0	1000	1000	0	0	0	0
0	14	0	1000	1000	0	0	0	0
0	15	0	1000	1000	0	0	0	0
0	16	0	1000	1000	0	0	0	0
0	17	0	1000	1000	0	0	0	0
0	18	0	1000	1000	0	0	0	0
0	19	0	1000	1000	0	0	0	0
0	20	0	1000	1000	0	0	0	0
0	21	0	1000	1000	0	0	0	0
0	22	0	1000	1000	0	0	0	0
0	23	0	1000	1000	0	0	0	0
0	24	0	1000	1000	0	0	0	0
0	25	0	1000	1000	0	0	0	0
0	26	0	1000	1000	0	0	0	0
0	27	0	1000	1000	0	0	0	0
0	28	0	1000	1000	0	0	0	0
0	29	0	1000	1000	0	0	0	0
0	30	0	1000	1000	0	0	0	0
0	31	0	1000	1000	0	0	0	0
0	32	0	1000	1000	0	0	0	0
0	33	0	1000	1000	0	0	0	0
0	34	0	1000	1000	0	0	0	0
0	35	0	1000	1000	0	0	0	0
0	36	0	1000	1000	0	0	0	0
0	37	0	1000	1000	0	0	0	0
0	38	0	1000	1000	0	0	0	0
0	39	0	1000	1000	0	0	0	0
0	40	0	1000	1000	0	0	0	0
0	41	0	1000	1000	0	0	0	0
0	42	0	1000	1000	0	0	0	0
0	43	0	1000	1000	0	0	0	0
0	44	0	1000	1000	0	0	0	0
0	45	0	1000	1000	0	0	0	0
0	46	0	1000	1000	0	0	0	0
0	47	0	1000	1000	0	0	0	0
0	48	0	1000	1000	0	0	0	0
0	49	0	1000	1000	0	0	0	0
0	50	0	1000	1000	0	0	0	0
0	51	0	1000	1000	0	0	0	0
0	52	0	1000	1000	0	0	0	0
0	53	0	1000	1000	0	0	0	0
0	54	0	1000	1000	0	0	0	0
0	55	0	1000	1000	0	0	0	0
0	56	0	1000	1000	0	0	0	0
0	57	0	1000	1000	0	0	0	0
0	58	0	1000	1000	0	0	0	0
0	59	0	1000	1000	0	0	0	0
0	60	0	1000	1000	0	0	0	0
0	61	0	1000	1000	0	0	0	0
0	62	0	1000	1000	0	0	0	0
0	63	0	1000	1000	0	0	0	0
0	64	0	1000	1000	0	0	0	0
0	65	0	1000	1000	0	0	0	0
0	66	0	1000	1000	0	0	0	0
0	67	0	1000	1000	0	0	0	0
0	68	0	1000	1000	0	0	0	0
0	69	0	1000	1000	0	0	0	0
0	70	0	1000	1000	0	0	0	0
0	71	0	1000	1000	0	0	0	0
0	72	0	1000	1000	0	0	0	0
0	73	0	1000	1000	0	0	0	0
0	74	0	1000	1000	0	0	0	0
0	75	0	1000	1000	0	0	0	0
0	76	0	1000	1000	0	0	0	0
0	77	0	1000	1000	0	0	0	0
0	78	0	1000	1000	0	0	0	0
0	79	0	1000	1000	0	0	0	0
0	80	0	1000	1000	0	0	0	0
0	81	0	1000	1000	0	0	0	0
0	82	0	1000	1000	0	0	0	0
0	83	0	1000	1000	0	0	0	0
0	84	0	1000	1000	0	0	0	0
0	85	0	1000	1000	0	0	0	0
0	86	0	1000	1000	0	0	0	0
0	87	0	1000	1000	0	0	0	0
0	88	0	1000	1000	0	0	0	0
0	89	0	1000	1000	0	0	0	0
0	90	0	1000	1000	0	0	0	0
0	91	0	1000	1000	0	0	0	0
0	92	0	1000	1000	0	0	0	0
0	93	0	1000	1000	0	0	0	0
0	94	0	1000	1000	0	0	0	0
0	95	0	1000	1000	0	0	0	0
0	96	0	1000	1000	0	0	0	0
0	97	0	1000	1000	0	0	0	0
0	98	0	1000	1000	0	0	0	0
0	99	0	1000	1000	0	0	0	0
0	100	0	1000	1000	0	0	0	0

Refinement was continued with anisotropic temperature factors in the forms:

$$\exp \{ -(h^2\beta_{11} + k^2\beta_{22} + l^2\beta_{33} + 2hk\beta_{12} + 2hl\beta_{13} + 2kl\beta_{23}) \}$$

The restrictions on the thermal ellipsoids of the two sodium atoms in special positions on the twofold axis are that $\beta_{12} = \beta_{23} = 0$ (Levy, 1956). Because of the degeneracy between β_{11} and the scale factors (Lingafelter & Donohue, 1966), the latter were rescaled after each cycle but not refined in the least-squares process. A refinement cycle reduced the reliability index to $R_1 = 0.073$.

A three-dimensional difference Fourier synthesis calculated at this stage revealed generally well defined peaks in positions where hydrogen atoms were expected on the basis of stereochemical considerations. The hydrogen atoms were included in the structure-factor calculations with isotropic temperature factors $B = 5.0 \text{ \AA}^2$. After two refinement cycles in which the parameters of the hydrogen atoms were not refined, the reliability index decreased to $R_1 = 0.062$, whereas $R_2 = [\sum w|F_o| - |F_c|^2 / \sum w|F_o|^2]^{1/2}$ was 0.063. Unit weights were assigned initially, but at the beginning of the anisotropic refinement the value of ΔF vs. F_o , was introduced:

$$w = 0 \text{ for unobserved reflexions}$$

$$w = \frac{F_o}{50.0} \text{ for } F_o \leq 50.0$$

$$w = \frac{50.0}{F_o} \text{ for } F_o > 50.0$$

The reflexion $60\bar{2}$ was excluded from the refinement, being too strong on the last film.

The shifts of all the parameters in the last cycle were well within their standard deviations, with an average $\Delta/\sigma = 0.4$, Δ being the change in a parameter in the last least-squares cycle and σ the e.s.d. of the parameter in that cycle.

The scattering factors used in the structure-factor calculations were taken from *International Tables for X-ray Crystallography* (1962). The observed and calculated factors are compared in Table 3. Table 4 gives the final positional and thermal parameters of all the atoms with their standard deviations.

Description and discussion of the structure

The principal structural features of sborgite are illustrated in Fig. 1, in which the structure is described in terms of boron coordination triangles and tetrahedra. Assignment of the hydrogen atoms can be made assuming, according to Christ's (1960) third rule, that the oxygen atoms O(1), O(3), O(8) and O(10), not shared between two boron atoms in the pentaborate ion, represent hydroxyl groups, and that the three unattached oxygen atoms O(11), O(12) and O(13)

the positions of all the heavy atoms in the structure. The coordinates of the heavy atoms as read from the E map were then refined by the full-matrix least-squares program ORFLS of Busing, Martin & Levy (1962) in the X-ray 70 System (Stewart, 1970). Individual scale factors for each layer were varied during the refinement; their starting values were those obtained by the DATFIX program. After three refinement cycles with isotropic temperature factors the value of the reliability index, defined as $R_1 = \sum |F_o| - |F_c| / \sum |F_o|$, was 0.11.

Table 4. *Positional and thermal parameters for heavy atoms and positional parameters for hydrogen atoms*Standard deviations are given in parentheses. Values for the heavy atoms are multiplied by 10^4 and for the hydrogen atoms by 10^3 .

	<i>x</i>	<i>y</i>	<i>z</i>	β_{11}	β_{22}	β_{33}	β_{12}	β_{13}	β_{23}
Na(1)	0	1528 (2)	2500	44 (3)	20 (1)	26 (2)	0	10 (2)	0
Na(2)	5000	1228 (2)	2500	185 (6)	23 (1)	34 (2)	0	56 (3)	0
O(1)	4038 (4)	2925 (2)	259 (3)	73 (4)	29 (2)	25 (2)	14 (2)	18 (2)	1 (1)
O(2)	2264 (3)	3827 (2)	-384 (2)	69 (4)	26 (2)	17 (2)	12 (2)	12 (2)	3 (1)
O(3)	413 (3)	4635 (2)	-1098 (2)	79 (4)	34 (2)	10 (2)	22 (2)	-9 (2)	2 (1)
O(4)	3281 (3)	3561 (2)	1487 (2)	52 (4)	21 (1)	19 (2)	6 (2)	8 (2)	2 (1)
O(5)	1406 (3)	4448 (2)	798 (2)	42 (4)	22 (1)	15 (2)	8 (2)	3 (2)	-1 (1)
O(6)	1979 (3)	3784 (2)	2491 (2)	49 (4)	20 (1)	16 (2)	-8 (2)	3 (2)	-5 (1)
O(7)	3291 (3)	4874 (2)	2278 (2)	54 (4)	18 (1)	13 (2)	-10 (2)	2 (2)	-1 (1)
O(8)	2189 (3)	3449 (2)	4259 (2)	73 (4)	32 (2)	22 (2)	-21 (2)	15 (2)	1 (1)
O(9)	3612 (3)	4403 (2)	4018 (2)	43 (4)	20 (1)	17 (2)	-15 (2)	2 (2)	0 (1)
O(10)	4750 (3)	5562 (2)	3755 (2)	59 (4)	21 (1)	24 (2)	-18 (2)	9 (2)	-1 (1)
O(11)	158 (3)	2609 (2)	1386 (2)	42 (4)	23 (1)	31 (2)	-4 (2)	13 (2)	-4 (1)
O(12)	2278 (3)	1422 (2)	3588 (3)	55 (4)	20 (1)	34 (2)	-4 (2)	8 (2)	-4 (1)
O(13)	3998 (3)	2271 (2)	3014 (3)	64 (4)	29 (2)	33 (2)	-1 (2)	15 (3)	4 (2)
B(1)	2500 (5)	4161 (3)	1769 (4)	42 (7)	21 (2)	9 (3)	1 (3)	0 (3)	3 (2)
B(2)	3212 (6)	3433 (4)	480 (4)	37 (6)	17 (2)	34 (3)	3 (3)	19 (4)	-1 (2)
B(3)	1387 (6)	4310 (4)	-189 (4)	43 (7)	20 (2)	22 (3)	1 (3)	8 (4)	4 (2)
B(4)	2552 (6)	3863 (4)	3571 (4)	58 (7)	17 (2)	17 (3)	-2 (3)	12 (3)	-2 (2)
B(5)	3867 (5)	4940 (3)	3358 (4)	41 (6)	18 (2)	16 (3)	-3 (3)	5 (3)	-3 (2)

Table 4 (cont.)

H(1)	477	267	89
H(3)	-18	490	-81
H(8)	121	316	400
H(10)	485	556	453
H(111)	91	301	162
H(112)	36	240	74
H(121)	236	149	436
H(122)	242	77	353
H(131)	379	268	250
H(132)	327	215	327

represent water molecules: these assignments were confirmed by the difference Fourier synthesis. The structure can thus be described as made up of pentaborate ions linked to each other either directly through hydrogen bonds or through sodium ions and water molecules.

Pentaborate group

The pentaborate ion, characterized by the double ring built up from one BO_4 tetrahedron and three BO_3 triangles, was first found by Zachariassen (1937) in $\text{KB}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$ and is also present in its ammonium analogue $\text{NH}_4\text{B}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$. More recently it was also found in $\beta\text{-NH}_4\text{B}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$ (Merlino, 1969).

Bond lengths and angles in the pentaborate group are reported in Table 5 and Fig. 2. The average B-O distance in the triangles is 1.361 Å and in the tetrahedron 1.468 Å, in good agreement with the results previously found in other borates by various workers. In Table 6 the average boron-oxygen bond lengths in sborgite are compared with the corresponding values found in $\text{KB}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$ (Zachariassen & Plettinger, 1963) and in $\beta\text{-NH}_4\text{B}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$. In this Table O^b and O^{nb} represent respectively oxygen atoms linked to two boron atoms in the trigonal state (bridging oxygen atoms), and oxygen atoms linked to only

one boron in the trigonal state (non-bridging oxygen atoms). The average B-O^b and B-O^{nb} distances are appreciably different in all three compounds. Coulson (1964, 1969) and Coulson & Dingle (1968) explain the difference of bond lengths of trigonal B-O bonds in terms of differences in π -bond order, which should clearly be smaller for a B-O^b bond than for a B-O^{nb} bond: Coulson & Dingle (1968), using the simple Hückel theory, obtained π -bond orders of 0.447 and 0.512 for B-O^b and B-O^{nb} respectively. On the other hand Zachariassen (1963) used Pauling's valence neutralization concept to explain the variations in B-O bond lengths. In fact in the case of sborgite two B-O^{nb} bonds, that is B(3)-O(3) (1.393 Å) and B(5)-O(10) (1.376 Å) are longer than the adjacent B-O^b bonds, that is B(3)-O(2) (1.362 Å) and B(5)-O(9) (1.364 Å).

Table 5. *Bond lengths and angles in the pentaborate group*

E.s.d.'s are given in parentheses.

Triangularly coordinated boron

Distance	Angle
B(2)-O(1)	O(1)-B(2)-O(2)
B(2)-O(2)	O(1)-B(2)-O(4)
B(2)-O(4)	O(2)-B(2)-O(4)
B(3)-O(2)	O(2)-B(3)-O(3)
B(3)-O(3)	O(2)-B(3)-O(5)
B(3)-O(5)	O(3)-B(3)-O(5)
B(4)-O(6)	O(6)-B(4)-O(8)
B(4)-O(8)	O(6)-B(4)-O(9)
B(4)-O(9)	O(8)-B(4)-O(9)
B(5)-O(7)	O(7)-B(5)-O(9)
B(5)-O(9)	O(7)-B(5)-O(10)
B(5)-O(10)	O(9)-B(5)-O(10)

Tetrahedrally coordinated boron

B(1)-O(4)	O(4)-B(1)-O(5)	110.4 (4)°
B(1)-O(5)	O(4)-B(1)-O(6)	108.7 (4)
B(1)-O(6)	O(4)-B(1)-O(7)	110.8 (4)
B(1)-O(7)	O(5)-B(1)-O(6)	109.3 (4)
	O(5)-B(1)-O(7)	107.3 (4)
	O(6)-B(1)-O(7)	110.2 (4)

Table 6. Average boron–oxygen bond lengths in sborgite, $\text{KB}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$ and $\beta\text{-NH}_4\text{B}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$

Compound	Triangle		Tetrahedron
	B–O ^a	B–O ^{nb}	
$\text{NaB}_5\text{O}_6(\text{OH})_4 \cdot 3\text{H}_2\text{O}$	1.383 Å	1.361 Å	1.468 Å
$\text{KB}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	1.372	1.352	1.478
$\beta\text{-NH}_4\text{B}_5\text{O}_6(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	1.379	1.356	1.479

The differences in bond lengths are opposite to those calculated discussing only the molecular structure of the pentaborate ion, as in the case of the Coulson & Dingle treatment. These differences are explained by taking into account the crystal packing effect, as in the Pauling–Zachariasen method of the balancing of valences. The lengthening of B(3)–O(3) and B(5)–O(10) bonds relative to the other B–O^{nb} bonds is then related

to Na–O bonds which O(3) and O(10) make with Na(2) and Na(1) respectively (for the balance of valences see below). Thus the situation is very similar to that found in the field of silicate structures where the variations in the Si–O distances can be explained in terms of *d*–*p* π -bonding as suggested by Cruickshank (1961), or on the basis of the Pauling–Zachariasen method of the balancing of valences. However for both Si–O bonds and trigonal B–O bonds the two theories are not necessarily exclusive and we can say, in accordance with Pant (1968), that π -bonding in trigonal B–O bonds ‘may be part of the mechanism whereby valency balance is achieved’.

The least-squares planes for the B_2O_5 groups formed by the coordination triangles are given in Table 7. The planes of the two B_2O_5 groups make an angle of 87.1° .

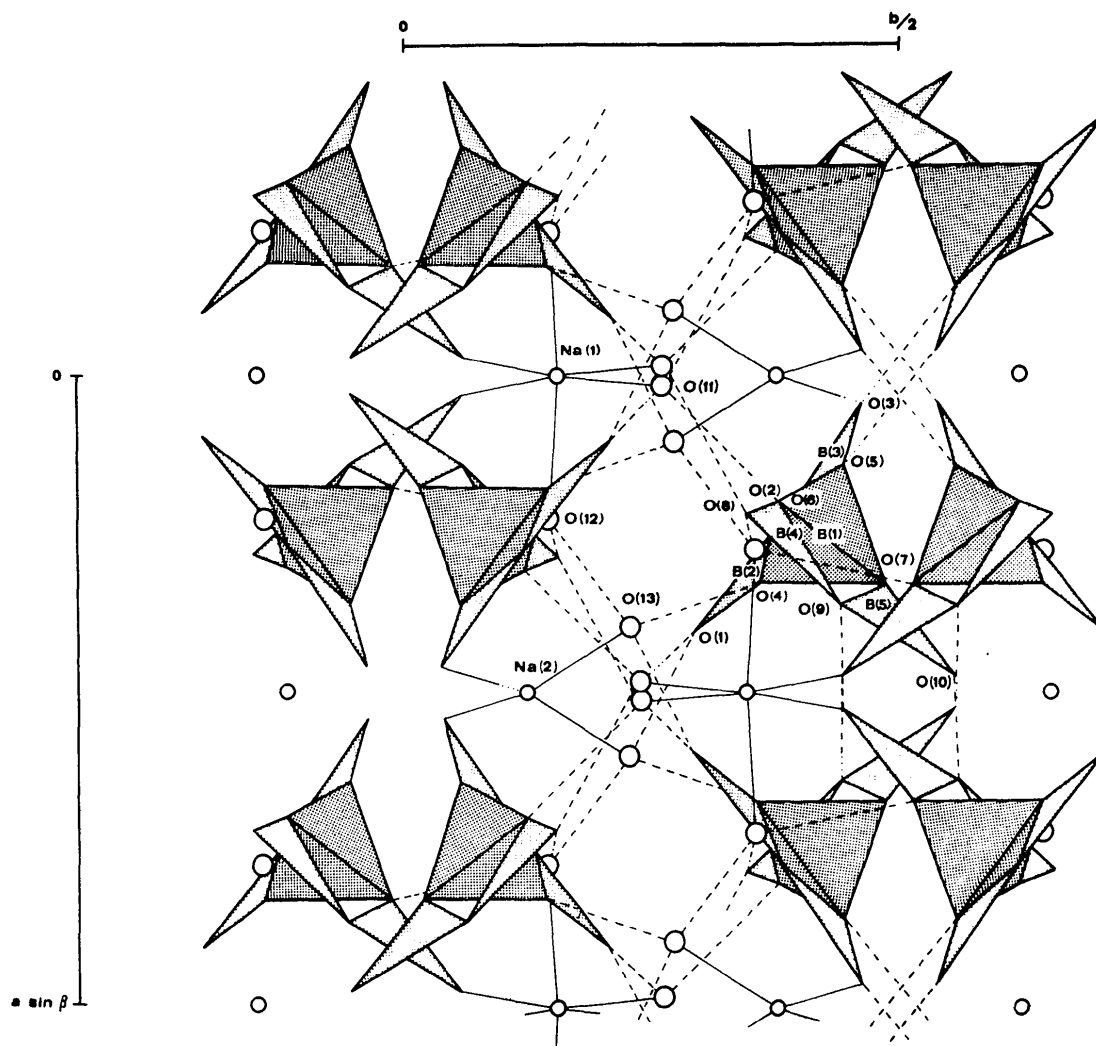


Fig. 1. The crystal structure of sborgite viewed along [001]. The continuous lines represent Na–O bonds; the dashed lines represent hydrogen bonds. Continuous and dashed lines ending with dots indicate that the bond is associated with an oxygen atom translated one unit in the [001] direction.

Symmetry code used in Tables 7, 8 and 9.

None	x	y	z
i	$-\frac{1}{2}+x$	$-\frac{1}{2}+y$	z
ii	$1-x$	$1-y$	$1-z$
iii	$-x$	$1-y$	$-z$
iv	$\frac{1}{2}-x$	$\frac{1}{2}-y$	$1-z$
v	$\frac{1}{2}-x$	$\frac{1}{2}-y$	$-z$
vi	$\frac{1}{2}+x$	$\frac{1}{2}-y$	$\frac{1}{2}+z$
vii	$1-x$	y	$\frac{1}{2}-z$
viii	$-x$	y	$\frac{1}{2}-z$
ix	$\frac{1}{2}-x$	$-\frac{1}{2}+y$	$\frac{1}{2}-z$

Sodium coordination

The two sodium ions in the asymmetric unit are in special positions on a binary axis. Na(1) is octahedrally coordinated by two O(10) hydroxyl ions and by four water molecules with a mean Na-O distance of 2.401 Å. The value is in very good agreement with the value 2.398 Å for $^{23}\text{Na}-^{16}\text{O}$ obtained on the basis of the effective ionic radii given by Shannon & Prewitt (1969). The Na(2) ion is coordinated tetrahedrally by two O(3) hydroxyl ions and two O(13) water molecules, with two other O(2) oxygen ions at a much larger distance (2.998 Å) corresponding to a valence bond strength of 0.03, calculated by the method of Donnay & Allmann (1970): we can thus assume that Na(2) has a coordination number four with two hydroxyl ions and two water molecules at the corners of an elongated tetrahedron (Fig. 1). Sodium with coordination number four has been found so far only in the crystal structures of Na_2O (Wyckoff, 1963), $\text{Na}_5\text{P}_3\text{O}_{10}$ (Corbridge, 1960) and $\text{NaOH} \cdot \text{H}_2\text{O}$ (Wunderlich, 1957). Na_2O has the anti-fluorite structure: sodium is in tetrahedral coordination, but the Na-O distances are not known. The sodium coordination in sodium triphosphate is very irregular, the Na-O distances ranging from 2.22 to 2.68 Å with a mean value of 2.37 Å. In the crystal structure of $\text{NaOH} \cdot \text{H}_2\text{O}$ there are pairs of edge-sharing sodium tetrahedra with Na-O bond lengths of 2.30, 2.35, 2.39 and 2.41 Å; the last two distances correspond to the oxygen atoms shared by two sodium atoms. From these data Shannon & Prewitt (1969)

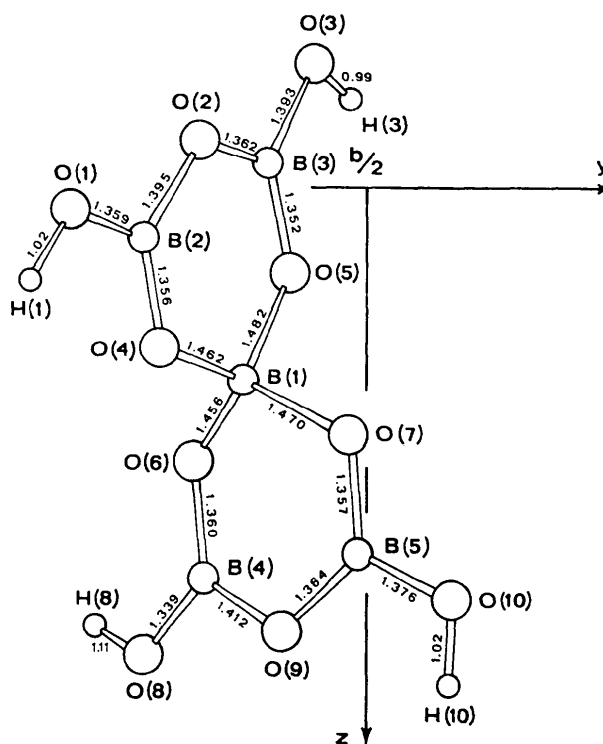


Fig. 2. Bond lengths in the pentaborate group. The group is viewed along [100].

derived for $^{14}\text{Na}^+$ an effective ionic radius of 0.99 Å, but they considered this doubtful, probably in view of the high irregularity of coordination in the case of $\text{Na}_5\text{P}_3\text{O}_{10}$ and the low accuracy of the data in the case of $\text{NaOH} \cdot \text{H}_2\text{O}$; in fact the value shows a strong deviation from the radii *vs.* coordination number plot.

Thus it seemed useful, in view of the substantially tetrahedral coordination of Na(2) and the good accuracy of the present determination, to calculate a value for the effective ionic radius of $^{14}\text{Na}^{+1}$ from our data. Taking into account that O(3) and O(13) have coordination numbers three (radius 1.357 Å) and four

Table 7. Mean-plane parameters and deviations of atoms from the plane

The equation of the plane is in the form $Ax + By + Cz = D$, where x , y , and z are fractional coordinates, calculated after Schomaker, Waser, Marsh & Bergman (1959).

Plane	A	B	C	D	Atoms defining the plane
I	6.8903	12.8523	-2.1924	6.5145	O(1), O(2), O(3), O(4), O(5), B(2), B(3)
II	-8.3247	10.9099	3.5706	3.3785	O(6), O(7), O(8), O(9), O(10), B(4), B(5)
III	-5.8393	13.8760	1.2499	1.1576	O(1 ^{iv}), O(8 ^{iv}), O(11 ^{vi}), O(12), O(13)

Deviations from plane

I		II		III	
O(1)	-0.029 Å	O(6)	-0.005 Å	O(1 ^{iv})	-0.013 Å
O(2)	0.050	O(7)	0.011	O(8 ^{iv})	-0.071
O(3)	-0.035	O(8)	0.084	O(11 ^{vi})	0.053
O(4)	-0.003	O(9)	-0.145	O(12)	0.066
O(5)	-0.006	O(10)	0.072	O(13)	-0.036
B(2)	0.005	B(4)	-0.010	H(1 ^{iv})	-0.007 Å
B(3)	0.019	B(5)	-0.007	H(8 ^{iv})	0.067
				H(112 ^{vi})	-0.038
				H(121)	-0.077
				H(132)	-0.325

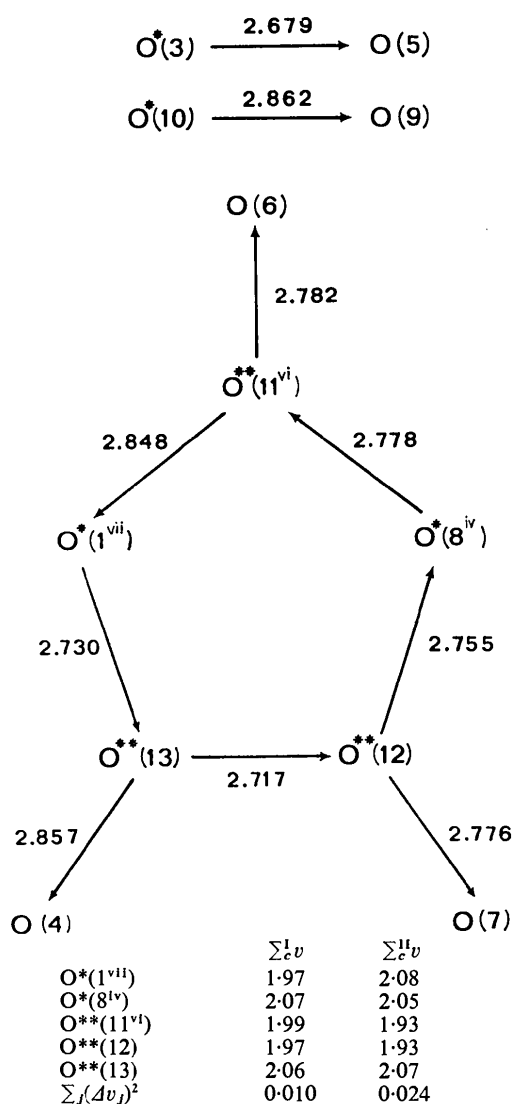


Fig. 3. Hydrogen-bond system. The valence sums are given for each anion of the pentagonal ring. $\sum_c^I v$ and $\sum_c^{II} v$ correspond respectively to the left-handed and the right-handed system of arrows in the ring. $\Delta v_j = (\sum_c v)_j - 2.0$ is the deviation from the ideal value 2.0 of the valence sum of the j th oxygen atom.

(radius 1.378 Å) respectively, from the bond lengths Na(2)–O(3) 2.276 and Na(2)–O(13) 2.298 Å we calculate the values 0.919 and 0.920 Å respectively; thus the value 0.92 Å for the effective ionic radius of $^{IV}\text{Na}^{+1}$ can be assumed with good confidence.

Hydrogen bond system

From a list of all the distances shorter than 3.0 Å between oxygen atoms not bonded to the same cation, the system of hydrogen bonds given in Fig. 3 can be deduced. In this figure the oxygen atoms marked with one or two asterisks were indicated as hydroxyl ions and water molecules respectively by application of Christ's third rule.

An interesting feature of the hydrogen bond system in sborgite is the presence of pentagonal rings, which characterize the structures of the clathrate hydrates (Pauling, 1960). For the hydrogen bonds external to the pentagonal ring donor and acceptor oxygen atoms can be unambiguously indicated. But for the hydrogen bonds of the pentagonal ring there is, beside the possibility indicated in the Figure (where the arrows go from the donor to the acceptor atoms), another possibility obtained by reversing the sense of the arrows in the ring. To test which of the two possibilities is correct we calculated the bond valence sums using the method of Donnay & Allmann (1970). In calculating hydrogen-bond valence strengths, use was made of the correlation between strength and length of hydrogen bonds given by Zachariasen (1963). The valence sum values for the five oxygen atoms of the ring strongly indicate that the first possibility (that represented in the Figure) for the hydrogen-bond system is the correct one. This was fully confirmed by a difference Fourier synthesis which showed well defined peaks in the predicted positions. Although in the present case the positions of the hydrogen atoms can be obtained from a difference synthesis, we think that in other less favourable cases the method of valence-sum calculations for testing the different possibilities of a hydrogen-bond system could be very useful.

The planarity of the pentagonal ring was tested by calculating the least-squares plane through the five

Table 8. Bond lengths and angles in the sodium coordination polyhedra

	Distance		Angle
Na(1)–O(11)	2.385 (4) Å	O(11)–Na(1)–O(11 ^{viii})	83.5 (2)°
Na(1)–O(11 ^{viii})	2.385 (4)	O(11)–Na(1)–O(12)	97.2 (1) [× 2]
Na(1)–O(12)	2.393 (4)	O(11)–Na(1)–O(12 ^{viii})	89.1 (1) [× 2]
Na(1)–O(12 ^{viii})	2.393 (4)	O(11)–Na(1)–O(10 ⁱ)	172.7 (2) [× 2]
Na(1)–O(10 ⁱ)	2.425 (4)	O(11)–Na(1)–O(10 ^{ix})	89.3 (1) [× 2]
Na(1)–O(10 ^{ix})	2.425 (4)	O(12)–Na(1)–O(10 ⁱ)	84.3 (1) [× 2]
		O(12)–Na(1)–O(12 ^{viii})	171.6 (2)
		O(12)–Na(1)–O(10 ^{ix})	90.2 (1) [× 2]
		O(10 ⁱ)–Na(1)–O(10 ^{ix})	97.9 (2)
Na(2)–O(13)	2.298 (5) Å	O(13)–Na(2)–O(13 ^{vii})	83.3 (2)°
Na(2)–O(13 ^{vii})	2.298 (5)	O(13)–Na(2)–O(3 ^v)	139.2 (1) [× 2]
Na(2)–O(3 ^v)	2.276 (4)	O(13)–Na(2)–O(3 ^{vi})	100.2 (1) [× 2]
Na(2)–O(3 ^{vi})	2.276 (4)	O(3 ^v)–Na(2)–O(3 ^{vi})	102.7 (2)
Na(2)–O(2 ^v)	2.998 (3)		
Na(2)–O(2 ^{vi})	2.998 (3)		

oxygen atoms. From the data of Table 7 it appears that the five hydrogen atoms involved in the five hydrogen bonds of the ring also lie approximately in the plane.

Bond lengths and angles involving hydrogen atoms were calculated assuming the coordinates obtained from the difference synthesis and are presented in Table 9. O—H bond lengths range from 0.93 to 1.11 Å with a mean value 1.03 Å.

Table 9. Distances and angles involving hydrogen atoms

Hydrogen bond O—H···O	Distances			Angles O—H···O
	O—H	H···O	O···O	
O(3)—H(3)···O(5 ^{III})	0.99 Å	1.74 Å	2.679 Å	157°
O(10)—H(10)···O(9 ^{II})	1.02	2.05	2.862	135
O(1)—H(1)···O(13 ^{VII})	1.02	1.72	2.730	178
O(13)—H(131)···O(4)	0.93	1.93	2.857	176
O(13)—H(132)···O(12)	1.02	1.79	2.717	149
O(12)—H(122)···O(7 ^{IX})	1.09	1.83	2.776	143
O(12)—H(121)···O(8 ^{IX})	1.02	1.75	2.755	169
O(8)—H(8)···O(11 ^{VIII})	1.11	1.67	2.778	172
O(11)—H(111)···O(6)	1.02	1.83	2.782	155
O(11)—H(112)···O(1 ^V)	1.04	1.81	2.847	171
H—O—H angles				
H(111)—O(11)—H(112)	93°			
H(121)—O(12)—H(122)	103			
H(131)—O(13)—H(132)	116			

Chidambaram, Sequeira & Sikka (1964) proposed a classification of hydrates based on the type of coordination of lone-pair orbitals of water. The lone-pair coordination of the three water molecules in sborgite is of the same type *G* in this classification scheme; that is, one of the lone pairs of electrons on each water molecule is directed approximately toward a monovalent metal ion, Na^+ in the present case, and the other lone pair is engaged in a hydrogen bond.

Crystal packing

The bond valence sums, calculated following the method of Donnay & Allmann (1970), are given in Table 10 for all the oxygen atoms; O* and O** represent respectively hydroxyl ions and water molecules. Satisfactory sums, ranging from 1.94 to 2.10, were found for each oxygen atom.

The building up of the crystal structure of sborgite, represented in Fig. 1, can be described as follows: the pentaborate group with atoms at x, y, z is linked through two hydrogen bonds of type O(3)···O(5) to the group with atoms at $-x, 1-y, -z$, and through two other hydrogen bonds of the type O(9)···O(10) to the pentaborate group at $1-x, 1-y, 1-z$, thus giving a chain zigzagging along the [101] direction. An adjacent chain is generated by a *c*-glide plane; the connexion between the chains is effected by sodium coordination polyhedra. In fact Na(2) atoms on the one hand connect the two chains through two equivalent Na(2)—O(3) bonds and on the other hand are linked to two equivalent O(13) water molecules. In the same manner Na(1) atoms connect the chains through Na(1)—O(10) bonds and are linked to two equivalent O(11) water molecules. The pentaborate chains are thus connected in layers linked to each other through layers of O(11) and O(13) water molecules. A further connexion is made by the O(12) water molecule that is bonded to the Na(1) atom and makes three hydrogen bonds with the O(7) atom of one chain, the O(8) atom of the other chain, and the O(13) water molecule of the separating layer.

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Table 10. Bond valence sums in sborgite

	B(1)	B(2)	B(3)	B(4)	B(5)	Na(1)	Na(2)	H	Σv
O*(1)		1.02						0.95	1.97
O(2)		0.95	1.01						1.96
O*(3)			0.95				0.25	0.74	1.94
O(4)	0.76	1.03						0.18	1.97
O(5)	0.72		1.03					0.27	2.02
O(6)	0.77			1.02				0.21	2.00
O(7)	0.75				1.02			0.21	1.98
O*(8)				1.06				1.01	2.07
O(9)				0.92	1.00			0.18	2.10
O*(10)					0.98	0.16		0.82	1.96
O**(11)						0.17		1.82	1.99
O**(12)						0.17		1.80	1.97
O**(13)							0.25	1.81	2.06

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The Crystal Structure of Lidocaine Hydrochloride Monohydrate*

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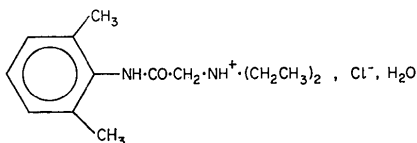
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Crystals of the title compound, $C_{14}H_{22}N_2O \cdot HCl \cdot H_2O$, are monoclinic, $P2_1/c$, with $a = 8.490$ (5), $b = 7.110$ (5), $c = 27.58$ (2) Å, $\beta = 106.87$ (5)°, $Z = 4$. 2385 of a possible 2694 independent reflexions in the range $\sin \theta / \lambda \leq 0.59$ were observed and measured diffractometrically. The crystal structure was determined by symbolic addition procedures and refined by block-diagonal least-squares calculations to a final R index of 0.11. There appears to be some disorder, with an alternative structure present at about 5% occupancy. Only the predominant structure has been characterized. This structure is fully hydrogen bonded, with adjacent lidocaine cations linked by water molecules into endless chains parallel to b . Adjacent chains related by the screw axes are joined in pairs by chloride ions, which bind N^+H and H_2O groups in different chains.

Introduction

The hydrogen-bonding properties of lidocaine in the hydrohexafluoroarsenate salt (I) have been studied by means of a determination of the crystal structure (Hanson, 1972). It also seemed of interest to study these properties in the hydrochloride monohydrate (II), as the environment of the lidocaine cation could be expected to approximate more closely the physiological environment in which it functions as a local anaesthetic. The hydrogen-bonding arrangement, and the conformation of the lidocaine cation, are found to be quite different in the two salts.



(II)

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Experimental

Crystal data: F.W. 288.8, $V = 1593$ Å³, $D_m = 1.21$, $D_x = 1.20$ g.cm⁻³, $\mu = 21.3$ cm⁻¹ (Cu $K\alpha$). [The wavelength assumed for $\lambda(\alpha_1)$ was 1.54050 Å.] The space group was determined by the systematic absences evident on Weissenberg and precession photographs.

The material supplied (Astra Pharmaceuticals Ltd.) was recrystallized from a solution in ethyl acetate and acetone, yielding colourless translucent prisms. These were generally of high mosaicity, and many were twinned. The nominal dimensions of the specimen used were $0.42 \times 0.31 \times 0.45$ mm. Cell dimensions and relative intensities were measured with a four-circle diffractometer and scintillation counter, using nickel-filtered Cu $K\alpha$ radiation with pulse-height discrimination. For the intensity measurements the specimen was mounted with c parallel to the ϕ axis; the θ - 2θ scan mode was used (scans of 3° for $2\theta \leq 50^\circ$, 4° for $50^\circ < 2\theta \leq 100^\circ$, 4.6° for $100^\circ < 2\theta \leq 130^\circ$) with background counts measured at the beginning and end of each scan. Reflexions for which the net count was less than 7 (deca-) counts or less than 10% of the corresponding background count were considered to be unobserved. The intensities were corrected for absorp-